

# An analytical model for budget allocation in risk prevention and risk protection

Xin Guan, Tom Servranckx, Mario Vanhoucke

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if you want to refer to this presentation, please refer to :

- Guan, X., Servranckx, T. and Vanhoucke, M. (2021). An analytical model for budget allocation in risk prevention and risk protection. Working paper.

## OUTLINE

- Introduction
- Problem formulation
- Analytical optimality
- Risk examples
- Experiments
- Conclusion

# INTRODUCTION

## **Project Risk**

- Uncertain events or conditions
- Negative impact  
(project delay, budget overrun, failure ...)

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## **Risk response strategy**

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## **Measure**

- Expected loss  
= Risk Probability (P) \* Risk Loss (L)

## **Risk response strategy**

- Risk Prevention (reduce P)
- Risk Protection (reduce L)

# INTRODUCTION

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(project delay, budget overrun, failure ...)

## **Measure**

- Expected loss  
= Risk Probability (P) \* Risk Loss (L)

## **Risk response strategy**

- Risk Prevention (reduce P)
- Risk Protection (reduce L)

## **Research question:**

How to allocate budget among risk  
prevention and risk protection?

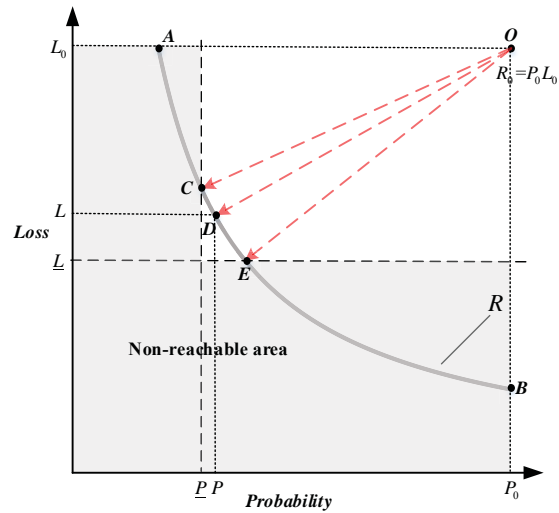
# PROBLEM FORMULATION

## – Problem statement

- initial risk ( $P_0, L_0, R_0$ )
- accepted risk level ( $R$ )  
→ risk response requirement
- minimal risk ( $\underline{P}, \underline{L}$ )  
→ risk controllability

## – Aim:

find the cheapest path from point O to curve CE?



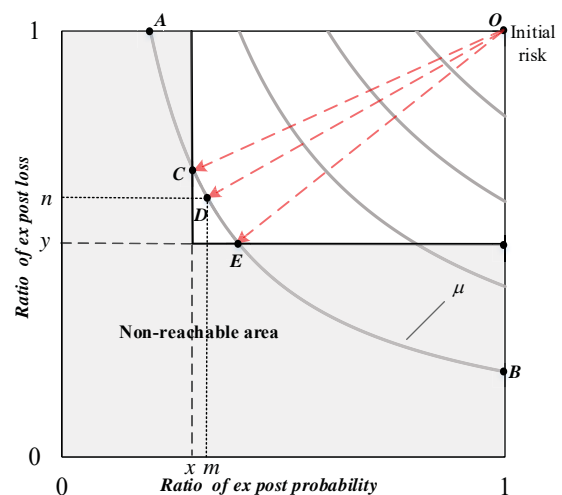
# PROBLEM FORMULATION

## – Problem statement

- initial risk ( $P_0, L_0, R_0$ )
- accepted risk level ( $R$ )  
→ risk response requirement ( $\mu = R/R_0$ )
- minimal risk ( $\underline{P}, \underline{L}$ )  
→ risk controllability ( $x = \underline{P}/P_0, y = \underline{L}/L_0$ )

## – Aim:

find the cheapest path from point O to curve CE?



# PROBLEM FORMULATION

## – Model formulation

– Relation between the cost (q, r) and effect (m, n) of risk response strategy:

– Linear:

– A higher risk reduction requires more budget

$$q = aP^0(1 - m) \qquad r = bL^0(1 - n)$$

– Nonlinear:

– After a certain risk reduction, further risk reduction requires a larger investment

$$q = aP^0 \ln \frac{1 - x}{m - x} \qquad r = bL^0 \ln \frac{1 - y}{n - y}$$

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– Model:

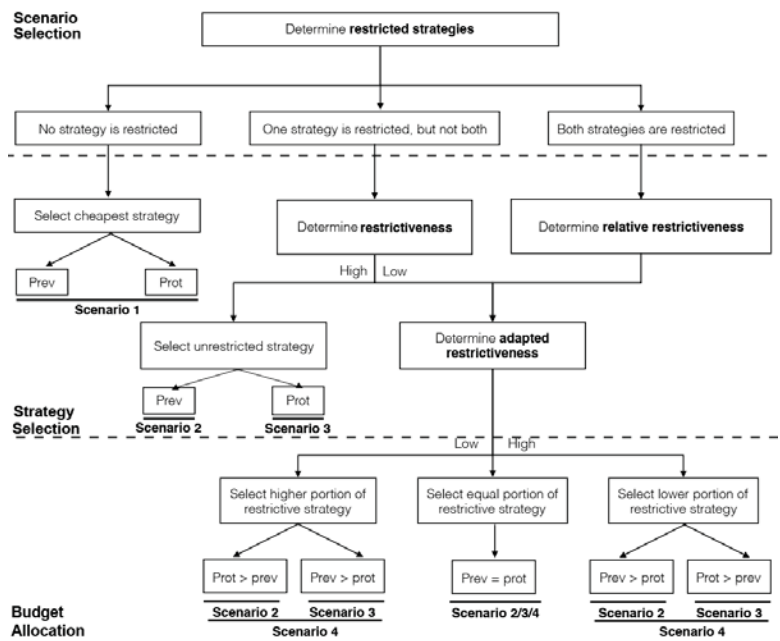
<b>LBAP</b> $\min \quad aP^0(1 - m) + bL^0(1 - n)$ $s. t. \quad mn = \mu$
--

<b>NBAP</b> $\min \quad aP^0(1 - m) + bL^0(1 - n)$ $s. t. \quad mn = \mu$
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# ANALYTICAL OPTIMALITY

## – 3-step decision procedure

- Step 1: Scenario selection
- Step 2: Strategy selection
- Step 3: Budget allocation

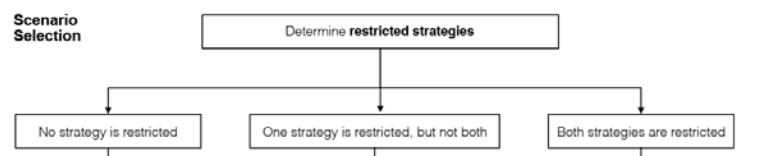


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# ANALYTICAL OPTIMALITY

## – 3-step decision procedure

- Step 1: Scenario selection
- risk response requirement vs risk controllability*



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# ANALYTICAL OPTIMALITY

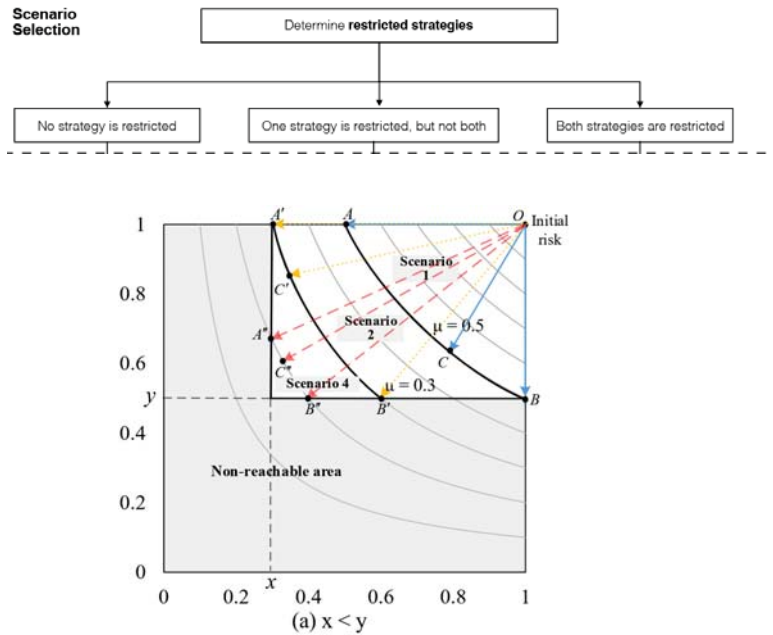
## – 3-step decision procedure

- Step 1: Scenario selection  
*risk response requirement vs risk controllability*

Example:

scenario 2:  $x < \mu < y$

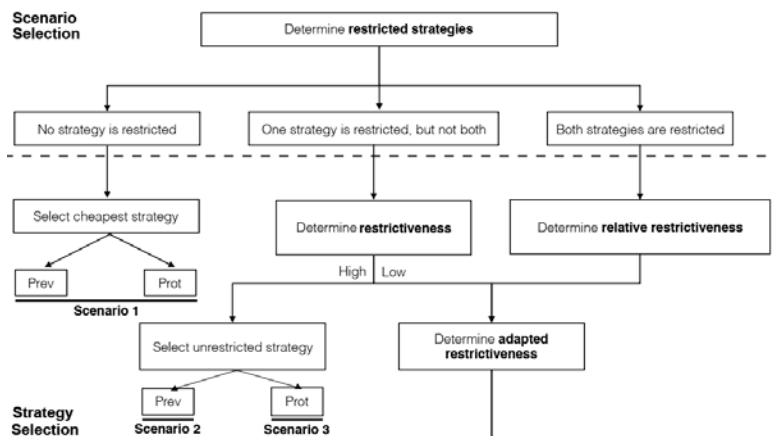
*risk protection is restricted.*



# ANALYTICAL OPTIMALITY

## – 3-step decision procedure

- Step 1: Scenario selection
- Step 2: Strategy selection  
*restrictiveness*  
*(a low value means a strong restrictiveness)*  
*risk prevention:  $\mu/x$*   
*risk protection:  $\mu/y$*



# ANALYTICAL OPTIMALITY

## – 3-step decision procedure

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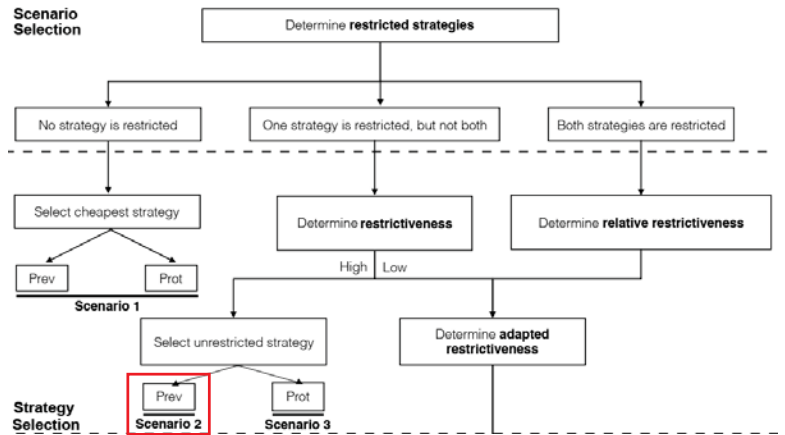
Example:

scenario 2:  $x < \mu < y$

risk protection is restricted,

if restrictiveness is high  $\rightarrow$  risk prevention

if restrictiveness is low  $\rightarrow$  both  $\rightarrow$  step 3



# ANALYTICAL OPTIMALITY

## – 3-step decision procedure

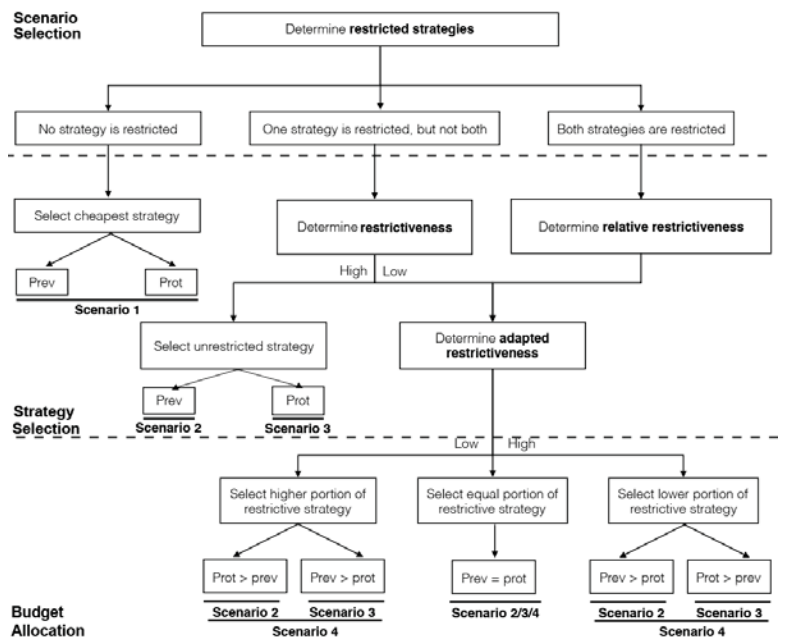
- Step 1: Scenario selection
- Step 2: Strategy selection
- Step 3: Budget allocation

*adapted restrictiveness*

(a low value means a low restrictiveness)

risk prevention:  $\frac{x - \mu}{x(1 - x)}$

risk protection:  $\frac{y - \mu}{y(1 - y)}$





# ANALYTICAL OPTIMALITY

## – 3-step decision procedure

- Step 1: Scenario selection
- Step 2: Strategy selection
- Step 3: Budget allocation

*adapted restrictiveness*

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$$\text{risk prevention: } \frac{x - \mu}{x(1 - x)}$$

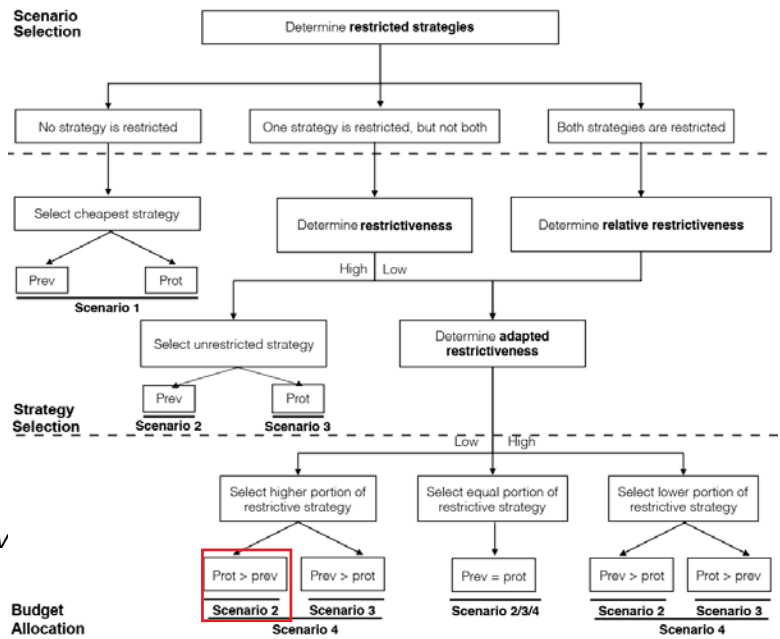
$$\text{risk protection: } \frac{y - \mu}{y(1 - y)}$$

Example: scenario 2:  $x < \mu < y$

risk protection is restricted,

if restrictiveness is low  $\rightarrow$  both,

if adapted restrictiveness is low  $\rightarrow$   $prot > prev$



# RISK EXAMPLES

Risk ID	Strategies from literature or practice	Budget allocation decision from model	
1	Acts of God. (extreme weather etc.)	• Buy insurance	Protection
2	People safety. (fall, exposure to harmful substances, etc.)	• Additional safety equipment, • Investment in training and protective materials • Insurance	Prevention
3	Potential conflicts between owner and stakeholders.	• Creating communication channels • Contract clauses, penalty clauses • Risk sharing	Protection > prevention
4	Poor schedules or unclear project scope.	• Regular meeting • Including buffer • Activity crashing • Reactive scheduling	Prevention > protection

# RISK EXAMPLES

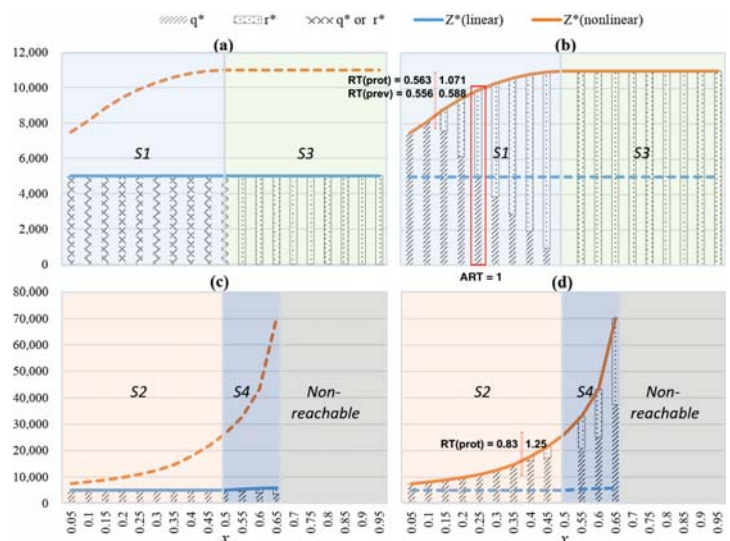
Risk ID		Strategies from literature or practice	Budget allocation decision from model
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2	People safety. (fall, exposure to harmful substances, etc.)	<ul style="list-style-type: none"> <li>Additional safety equipment,</li> <li>Investment in training and protective materials</li> <li>Insurance</li> </ul>	Prevention
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- Our model results are consistent with the strategies from literature or practice.

# EXPERIMENTS

## – Impact of risk controllability in probability (x)

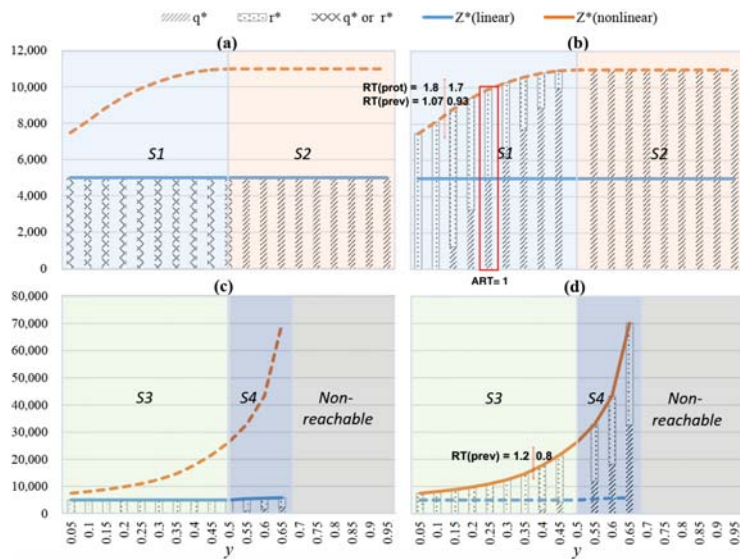
- the controllability has no significant effect on the optimal risk cost in the LBAP.
- In NBAP,
  - Scenarios 1 and 2, the impact of risk controllability is reflected on the restrictiveness and the adapted restrictiveness.
  - Scenario 3, the controllability in risk probability has no effect on the optimal risk cost since the complete budget is allocated to risk protection.
- Scenarios 2 and 4, a lower controllability in risk probability (a higher x) leads to a greater investment in risk prevention.



# EXPERIMENTS

– Impact of risk controllability in loss (y)

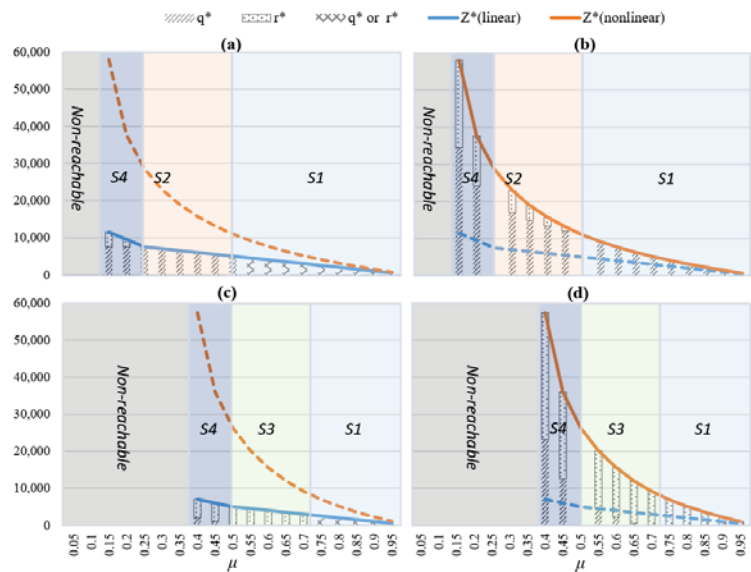
– Similar results are observed.



# EXPERIMENTS

– Impact of response requirement ( $\mu$ )

– A strict requirement always leads to a higher response cost.



# CONCLUSIONS

## – Conclusions

- A three-step decision-making process can be followed.  
(the risk response requirement, risk controllability, and the restrictiveness of strategies)
- A lower controllability in risk loss (probability) leads to a greater investment in risk prevention (protection).

## – Future research

- A more general case: relax the linear and nonlinear relations
- Multiple risks: extend to multiple risks and construct a risk network with complex relations

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